

FINAL EXAMINATION – JULY 2017
MASTER OF SCIENCE (M.Sc. MATHEMATICS)

First Year – First Semester
Real Analysis – I

1M.Sc. 2

Time : 3 Hours

Max Marks : 70

Min. Marks : 25

Note :- Solve any two parts from each question. All questions carry Equal marks.

- Q.1. (a) State and prove Cesaro's theorem.
(b) State and prove Nested interval theorem.
(c) If $\{S_n\}$ is a convergent sequence of real numbers and if $\lim S_n = l$, then prove that $\overline{\lim} S_n = \underline{\lim} S_n = l$ conversely, if $\overline{\lim} S_n = \underline{\lim} S_n = l \in R$, then prove that $\{S_n\}$ is convergent and $\lim_{n \rightarrow \infty} S_n = l$.

- Q.2. (a) State and prove Cauchy's condensation test.
(b) Test for convergence of the series
(i) $x + \frac{2^2 x^2}{2!} + \frac{3^3 x^3}{3!} + \frac{4^4 x^4}{4!} + \dots$
(ii) $\frac{1}{(\log 2)^p} + \frac{1}{(\log 3)^p} + \dots + \frac{1}{(\log n)^p} + \dots$
(c) State and prove D'Morgan and Bertrand's Test.

- Q.3. (a) State and prove general principle of convergence.
(b) Suitably deranging the series
$$S = 1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + \dots$$
Prove that $S = \frac{1}{2}S$. explain the fallacy.
(c) State and prove Euler's constant theorem.

- Q.4. (a) State and prove Bolzano - Weierstrass theorem.

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- (b) Prove that the real line \mathbb{R} is of the second category.
- (c) Prove that every closed and bounded set of real numbers is compact.

- Q.5. (a) State and prove Bolzano's theorem on continuity.
- (b) State and prove Darboux theorem.
 - (c) State and prove Cauchy's mean value theorem.

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