Course Code: 3MSCM1 Course: Functional Analysis-I Credit: 4 Last Submission Date: April 30 (for January Session) October 31, (for July session)

> Max. Marks:-70 Min. Marks:-25

Note:-attempt all questions.

- Que.1 Let X & Y be Banach spaces & T a continuous linear transformation of X onto Y thent is an open mapping.
- Que.2 State & prove Holder's & Minkowshki's inequality.
- Que.3 Let H be a separable infinite-dimensional complex Hilbert space. Then H is isometrically isomorphic to  $l_2$ .
- Que.4 If x(t),  $y(t) \in L_P(0,1)$  then  $x(t) \neq y(t) \in L_P(0,1)$
- Que.5 State & prove Hahn Banach theorem.
- Que.6 State & prove Uniform Boundedness theorem.
- Que.7 State & prove Riesz-lemma.
- Que.8 State & prove Convexity theorem.

Que.9 Let  $\{x_n\}$  be a weakly convergent sequence in a normal space X; i.e.  $x_n \xrightarrow{w} x$ . Then

- (1) Weak limit of the sequence  $\{x_n\}$  is unique.
- (2) Every subsequence of  $\{x_n\}$  converges weakly to x.
- (3) The sequence II  $x_n$  II is bounded.
- Que.10 State & prove Uniform boundedness theorem.