Course Code: 2MSCM3 Course: Topology-II Credit: 4 Last Submission Date: October 31, (for January session) April 30 (for July Session)

> Max. Marks:-70 Min. Marks:-25

Note:-attempt all questions.

- Que.1 Let F_1 , F_2 be any pair of disjoint closed sets in a normal space X. Then there exist a continuous mapping $f : X \rightarrow [0,1]$ such that f(x) = 0 for $x \in f_1$ & f(x) = 1 for $x \in f_2$
- Que.2 State & prove Tietze extension theorem.
- Que.3 Prove that every second countable space is first countable and converse not true.
- Que.4 Every second countable space is separable.
- Que.5 A continuous image of a sequentially compact set is sequentially compact.
- Que.6 Every closed subspace of a locally compact space is locally compact.
- Que.7 Let (X,d) be a complete metric space and let Y be a subspace of X. Then Y is complete if and only if Y is closed.
- Que.8 Every convergent sequence in a metric space is a Cauchy sequence.
- Que.9 The product space $X \times Y$ is connected if and only if X and Y are connected.
- Que.10 State & prove Tychonoff's theorem.