

Course Code: 1MSCM2
Course: Real Analysis-I
Credit: 4
Last Submission Date: April 30 (for January Session)
October 31, (for July session)

Max. Marks:-70
Min. Marks:-25

Note:-attempt all questions.

Que.1 Show that sequence $\left\{\frac{2n+3}{3n-2}\right\}$ is convergent.

Que.2 Prove that $\lim_{n \rightarrow \infty} \left\{\frac{x^n}{n}\right\} = 0$ if $|x| < 1$

Que.3 Test the convergence of the series

$$x + \frac{2^2 x^2}{2!} + \frac{3^3 x^3}{3!} + \dots$$

Que.4 Test the convergence or divergence of the series

$$1^p + \left(\frac{1}{2}\right)^p + \left(\frac{1.3}{2.4}\right)^p + \left(\frac{1.3.5}{2.4.6}\right)^p + \dots$$

Que.5 Suppose $g(x) = \sum_{n=0}^{\infty} c_n x^n$ be a power series which converges for $|x| < 1$, If

$$\sum_{n=0}^{\infty} c_n \text{ converges then } \lim_{x \rightarrow 1} g(x) = \sum_{n=0}^{\infty} c_n$$

Que.6 If $\sum u_n$ is convergent then $\lim_{n \rightarrow \infty} u_n = 0$

Que.7 State and prove Bolzano – weierstrass theorem.

Que.8 State & prove Baire category theorem for \mathbb{R} .

Que.9 State & prove Cauchy' mean value theorem.

Que.10 If $f(x, y) = \begin{cases} \frac{xy}{x^2+y^2}, & \text{for } (x, y) \neq (0, 0) \\ 0, & \text{for } (x, y) = (0, 0) \end{cases}$

Find $f_x(0, 0)$ and $f_y(0, 0)$