

Course Code: 1BSC4  
 Course: Mathematics-I  
 Credit: 4  
 Last Submission Date: April 30 (for January Session)  
 October 31, (for July session)

Max. Marks:-30  
 Min. Marks:-10

Note:-attempt all questions.

Que1. Determine the Eigen value and Eigenvectors of the given matrix

$$A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$

Que2. Find the roots of the equation  $x^2 - 3x^2 - 16x + 48 = 0$ , when the sum of two roots is zero.

Que3. Find all values of  $(1 + \sqrt[3]{3})^{10} + (1 - \sqrt[3]{3})^{10}$

Que4. Find the sum of the series

$$1 + \frac{\cos\theta}{\cos\theta} + \frac{\cos 2\theta}{\cos^2\theta} + \frac{\cos 3\theta}{\cos^3\theta} + \dots$$

Que5. Show that  $(\mathbb{Q}, +)$  is an abelian group, where  $\mathbb{Q}$  is the set of rational numbers.

Que6. State and prove Lagrange's theorem.

Que7. Define Homomorphism with example and state and prove second theorem on Homomorphism.

Que8. Show that  $(\mathbb{I}, +, \cdot)$  is a Ring, where  $\mathbb{I}$  is the set of integers.

Que9. Find the equation of the cone whose vertex is  $(5, 4, 3)$  and base curve  $3x^2 + 2y^2 = 6$ ,

$$Y + Z = 0$$

Que10. Find the equation of the cylinder whose generators are parallel to the

Whose generators are parallel to the

$$\text{Line } \frac{x}{1} = \frac{y}{2} = \frac{z}{3} \text{ and passing through}$$

$$\text{The curve } x^2 + y^2 = 16, y = 0$$